

UNIVERSITAT POLITÈCNICA DE CATALUNYA

*Departamento de Matematica Aplicada III, dentro del programa de
Doctorado de Matematica Aplicada*

**ESTUDIO SOBRE ALGUNAS
NUEVAS CLASES DE
CONECTIVIDAD CONDICIONAL
EN GRAFOS DIRIGIDOS**

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